

## Shri Vaishnav Vidyapeeth Vishwavidyalaya, Indore Name of the Program: B.Sc. in Mathematics

SUBJECT CODE			TEACH	ING & EV	ALUATI	ON SCHE	ME				
	Catagory	Category SUBJECT NAME	THEORY			PRACTICAL		Th	Т	P	Şo.
	Category		END SEM	MST	Q/A	END SEM	Q/A	111	,		CREDITS
MSMA201	DC	Abstract Algebra II	60	20	20	-	-	4	0	-	4

## **Course Objective**

To introduce the students to the basics of abstract Algebra.

### **Course Outcomes**

After the successful completion of this course, students will be able to:

- 1. apply the basics of the abstract algebra
- 2. understand the concept of Noetherian & Artinian modules
- 3. demonstrate knowledge and understanding of the concept of Modules and Submodules
- 4. to apply Hilbert basis theorem and Wedderburn-Artin theorem to solve problems of Algebra.

## Course Content:

Symmetric functions, Cyclotomic Extensions, Insolvability of Quintic. (5. Section 54, 55, 56)

Introduction to Modules, Examples, Submodules and direct sums, Cyclic module, R-homomorphisms and Quotient modules, Isomorphism.

(1. Chapter 14 Sections 1-3)

Chairperson **Board of Studies Physical Sciences** 

Chairperson **Faculty of Studies** Science

Controller of Examinations Shri Vaishnav Vidyapeeth Vishwavidyalaya, Indore



## Shri Vaishnav Vidyapeeth Vishwavidyalaya, Indore

## Name of the Program: B.Sc. in Mathematics

SUBJECT CODE			TEACH	ING & EV	ALUATI	ON SCHE	ME				
	Catego	ego SUBJECT NAME	THEORY			PRACTICAL		an.	Т	P	S
			END SEM	MST	Q/A	END SEM	Q/A	Th	,	•	CREDITS
MSMA201	DC	Abstract Algebra II	60	20	20	-	-	4	0	-	4

### **UNIT-III**

Completely reducible modules Schur's lemma, Free modules, Representation of linear mappings, Rank of linear mappings.

(1. Chapter 14 Sections 4 - 7)

### **UNIT-IV**

Noetherian & Artinian modules and rings, Hilbert basis theorem. Weddeburn-Artin theorem.

(1. Chapter 19 Sections 1-3)

### **UNIT-V**

Uniform modules, Primary, modules, finitely generated modules over a PID, Decomposition theorem, Uniqueness of the decomposition. Application to finitely generated abelian groups.

(1. Chapter 19 Sections 4, Chapter 21 Sections 1-3)

### References

- 1. P.B. Bhattacharya, S.K. Jain and S.R. Nagpaul, Basic Abstract Algebra, Cambridge University Press.
- 2. I.N. Herstein, Topics in Algebra, Wiley Eastern, New Delhi.
- 3. V. Sahai & V. Bisht, Algebra, Narosa Publishing House.
- 4. N. Jacobson, Basic Algebra I and II, 2nd Ed., W. H. Freeman, 1985 and 1989.
- 5. John B. Fraleigh, A First Course in Abstract Algebra, Narosa Publication.

**Board of Studies Physical Sciences**  **Faculty of Studies** Science

Controller of Examinations Shri Vaishnav Vidyapeeth Vishwavidyalaya, Indore



## Shri Vaishnav Vidyapeeth Vishwavidyalaya, Indore Name of the Program: B.Sc. in Mathematics

SUBJECT CODE		TEACHING & EVALUATION SCHEME									
	Category	SUBJECT NAME	THEORY			PRACTICAL					
			END SEM	MST	Q/A	END SEM	Q/A	Th	Т	P	CREDITS
MSMA202	DC	Theory of Measure and Integration	60	20	20	-	-	4	0	-	4

### **Course Objective**

To introduce the students to the Theory of Measure and Integration.

### **Course Outcomes**

fter the successful completion of this course, students will be able to:

- understand and apply the basics of the Theory of Measure and Integration.
- analyse and construct the outer measure, measurable sets, Lebesgue measure and measure space.
- apply the concepts of measure theory to probability theory.
- evaluate integrals beyond Riemann's integration theory.
- synthesize real-world applications of measure theory.

### Course Content:

 $F_{\sigma}$ ,  $G_{\delta}$  sets, Introduction to Lebesgue Outer Measure, Measurable sets and Lebesgue Measure, Non-Measurable sets.

1. Chapter 2 sections 7, Chapter 3 sections 1-4)

MInit II:

Measurable Functions, Egoroff's theorem, Lusin's theorem, Little-Wood's three Principles, A Non-Borel Measurable Set. The Riemann Integral, Lebesgue Integral of a Bounded Function over a set of Finite Measure.

(1. Chapter 3 sections 4 - 6, Chapter 4 sections 1, 2)

**Board of Studies Physical Sciences**  **Faculty of Studies** Science

Shri Vaishnav Vidyapeeth Vishwavidyalaya, Indore



# Shri Vaishnav Vidyapeeth Vishwavidyalaya, Indore

## Name of the Program: B.Sc. in Mathematics

SUBJECT CODE			TEACH	ING & EV.	ALUATI	ON SCHE	ME				
	Category	SUBJECT NAME	THEORY			PRACT			D	S	
			END SEM	MST	Q/A	END SEM	Q/A	Th	Т	P	CREDITS
MSMA202	DC	Theory of Measure and Integration	60	20	20	-	-	4	0	-	4

The Integral of a Non-Negative Function, The General Lebesgue Integral, Convergence in Measure, Differentiation of Monotone Functions, The Four Derivatives.

(l. Chapter 4 sections 3-5, chapter 5 section 1)

Functions of Bounded Variation, Differentiation of an Integral, Absolute Continuity, Convex Functions, Jensen Inequality. The LP-spaces, The Holder and Minkowski Inequalities.

(1. Chapter 5 sections 2 - 5, Chapter 6 sections 1, 2)

Convergence and Completeness, Riesz-Fischer Theorem, Approximation in LP, Bounded Linear Functionals on the LP-spaces, Riesz Representation Theorem.

(1. Chapter 6 sections 3 - 5)

### Reference Books:

- 2. Walter Rudin, Principles of Mathematical Analysis, McGraw-Hill, International Studen
- 3. G. De Barra. Measure Theory and Integration, Wiley Eastern (Indian Edition).
- 4. Inder K Rana, An Introduction to Measure and Integration, Second Edition, Narosa Publication
- 5. Lebesgue Measure and Integration, 2nd Edition by P.K. Jain, V.P. Gupta, Pankaj Jain

**Board of Studies Physical Sciences**  **Faculty of Studies** Science

Controller of Examinations Shri Vaishnav Vidyapeeth Vishwavidyalaya, Indore



## Shri Vaishnav Vidyapeeth Vishwavidyalaya, Indore Name of the Program: B.Sc. in Mathematics

SUBJECT CODE			TEACH	ING & EV	ALUATI	ON SCHE	ME				
	Category	OF SUBJECT NAME	THEORY			PRACT	TICAL		_		
			END SEM	MST		END SEM	Q/A	Th	Т	P	CREDITS
MSMA204	DC	Topology II	60	20	20			4	0	0	4

### **Course Objective**

To introduce the students to the basics of Topology.

### **Course Outcomes**

After completing the course the student will be able to:

- 5. understand and apply the concept of compactness
- 6. apply separable axioms
- 7. understand concepts of Nets and filter
- 8. analyse and apply the covering axiom and consequences
- 9. synthesis of basic topology to formulate and solve problems of a topological nature in mathematics and other fields where topological issues arise.

## Course Content:

Compactness, Continuous functions and compact sets, basic properties of compactness. Compactness and F.I.P. (Finite intersection property). Sequential and countably compact spaces. Local compactness and one-point compactification. Compactness in metric space. Equivalence of compactness. Countable compactness.

(1. Sections 26, 27, 28 and 29)

The Separation axioms. Regular and Normal spaces. Urysohn's Lemma. Tietze's Extension Theorem. (1. Section 31, 32 and 35)

Chairperson Board of Studies **Physical Sciences**  **Faculty of Studies** Science

Controller of Examinations Shri Vaishnav Vidyapeeth Vishwavidyalaya, Indore



### Shri vaishnav vidyapeeth Vishwavidyalaya, Indore

## Name of the Program: B.Sc. in Mathematics

SUBJECT CODE			TEACH	ING & EV	ALUATI	ON SCHE	ME				
	Category	SUBJECT NAME	THEORY			PRACT	TCAL		П		
			END SEM	MST	Q/A	END SEM	Q/A	Th	Т	P	REDITS
MSMA204	DC	Topology II	60	20	20	22	22	4	0	0	4

### Unit-III

Tychnoff product topology in terms of standard sub-base and its characterizations, Embedding and metrization. Embedding lemma and Tychnoff embedding. The Urysohn's metrization.

(1. Section 37) and (2. chapter 9)

### Unit -IV

Nets and filters. Topology and convergence of nets. Hausdorffness and nets. Compactness and nets. Filters and their convergence. Canonical way of converting nets to filters. Ultrafilters and compactness.

(2. Chapter 10 sections 1-4)

### Unit-V

The Fundamental group and covering spaces-Homotopy of paths. The Fundamental group. Covering spaces. The Fundamental group of the circle and the fundamental theorem of algebra.

(1. Sections 51, 52, 53, 54 and 56)

### Reference Books:

1. James R. Munkres: Topology, A First Course, Prentice Hall of India Pvt. Ltd.

New Delhi.

- 2. K. D. Joshi: Introduction to general Topology, Wiley Eastern Limited.
- 3. G. F. Simmons: Introduction to Topology and Modern Analysis. Mc-Graw Hill.

Chairperson **Board of Studies Physical Sciences**  **Faculty of Studies** Science

Controller of Examinations Shri Vaishnav Vidyapeeth Vishwavidyalaya, Indore